

# Multi-Objective Path Planning for a Team of Unmanned Aerial Vehicles (UAVs) in a Dynamic and Uncertain Environment

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- Technical Challenges
- Path Planning Framework
- Objectives & Constraints
  - Results



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- Hierarchical Mission Planning Framework
- Multi-Objective Path Planning for UAVs
- Problem Formulation
- Simulation Results
- Conclusion
- Future Work
- References

### **Introduction: UAV Mission Planning**

 UAVs have ultra long endurance and can accept high mission risk; these attributes make them suitable for dull, dirty, and dangerous tasks in complex environments:

#### - Military:

- Intelligence, Surveillance & Reconnaissance (ISR)
- Search and Rescue Operations (SAR)
- Demining Operations

#### - Security:

- Border Patrol
- Surveillance of Smuggling Operations
- Interdiction Operations

#### - Civil:

- Disaster Management
- Forest Fire Detection
- Traffic Monitoring











**Technical** Challenges

Path **Planning** Framework

Objectives Constraints

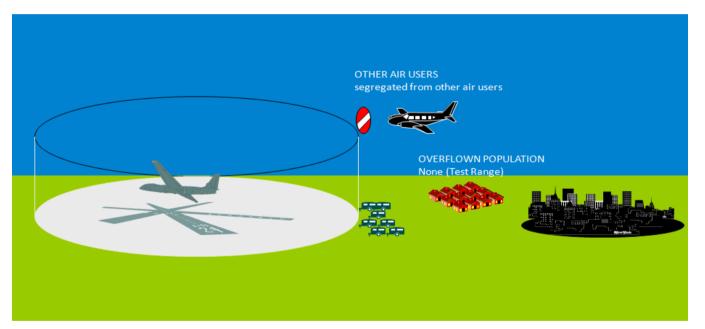
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 In the future, UAVs are expected to operate with a higher level of autonomy to carry out complex tasks, while efficiently coordinating with unmanned ground and unmanned underwater vehicles ⇒ Need for systematic mission planning processes

### **Technical Challenges**

- Lack of see and avoid capability:
  - May lead to mid-air collisions with manned vehicles
  - Restricts UAVs to operate in segregated regions in the airspace
  - Needs substantial human supervision
  - Limits operational flexibility



Flying UAV within national borders in controlled, segregated airspace over an unpopulated area

- Limited sensor ranges and payload capacity requires multiple UAVs to:
  - Work cooperatively
  - Expedite the mission execution
  - Reduce the possibility of mission failure



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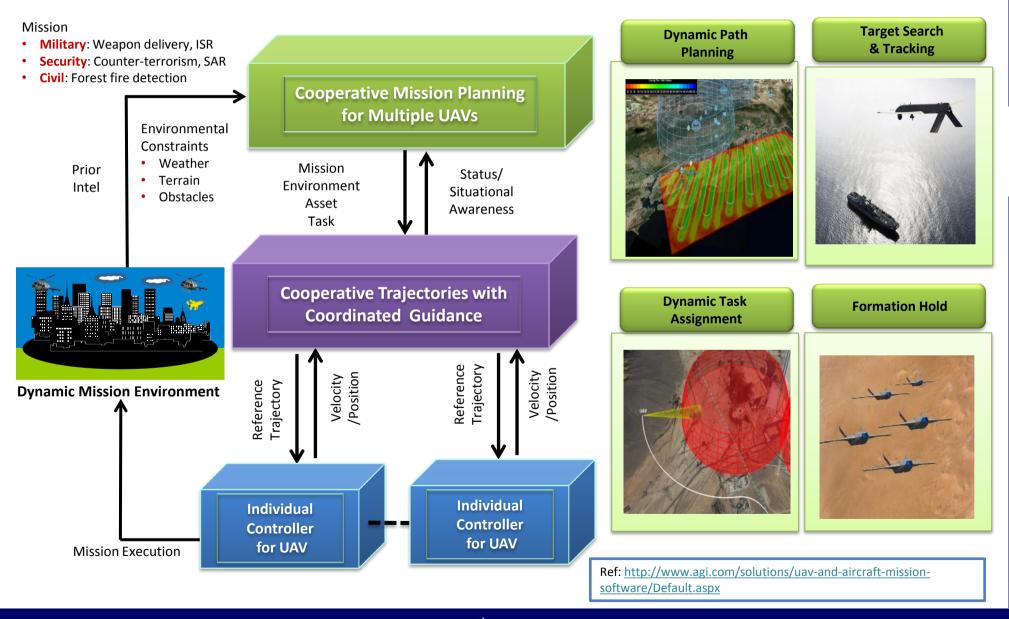
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### Hierarchical Architecture for UAV Mission Planning

Systematic mission planning structure for conducting complex tasks involving multiple UAVs





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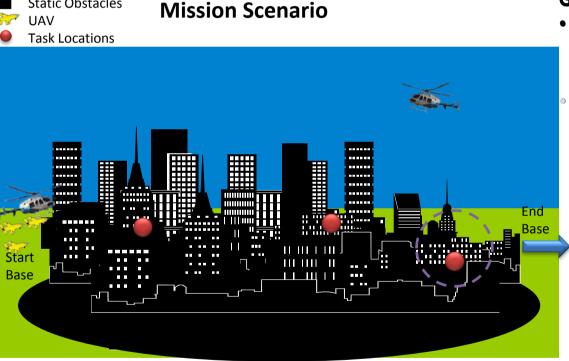
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### Multi-Objective Path Planning for UAVs

- **Objective**: Coordinated multi-objective path planning for a group of UAVs in a dynamic environment to carry out time-critical mission tasks:
  - Minimize mission risk (path cost, e.g., distance of UAV from obstacle)
  - Minimize task latencies

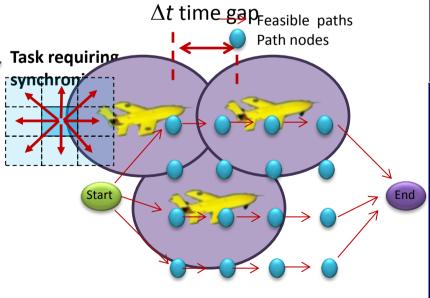


#### Given:

- Dynamic environment with static and dynamic obstacles, e.g., high rise buildings, manned aircraft
- Task locations, deadlines, task requirements

#### **Constraints:**

- **Mention floorist majors** traint
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**Time Horizon** 

**Task Deadlines** 

**Task Requirements** 

Dynamic Obstacles

Static Obstacles

### **UAV Path Planning Formulation**

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- Multi-Objective Mixed Integer Linear Programming (MILP) Problem:
  - Objective I: Minimize cumulative path risk Time varying travel and usage cost

$$Obj_{1} : \min_{x_{ijkt}} \sum_{t=1}^{T} \sum_{k=1}^{K} \sum_{(i,j) \in \Omega} r_{ijkt} x_{ijkt}$$

$$x_{ijkt} = \begin{cases} 1, & \text{if UAV } k \text{ moves from cell } i \text{ to cell } j \text{ at time } t \\ 0, & \text{otherwise} \end{cases}$$

where T is the time horizon, K is the total number of UAVs and  $\Omega$  is the set of accessible paths  $r_{iikt}$  is the path risk experienced by UAV k in moving from cell i to cell j at time t

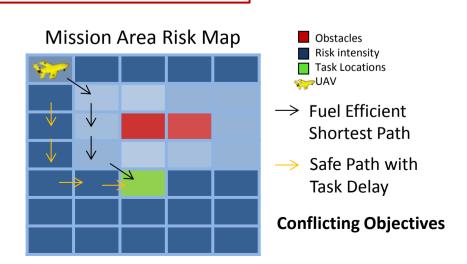
- Objective II: Minimize task latency - Delay in meeting the task deadline

$$Obj_{2}: \min \sum_{l=1}^{L} t_{l}^{latency}, \quad t_{l}^{latency} = \max(0, t_{l}^{start} + t_{l}^{process} - t_{l}^{deadline})$$
 (2)

where

 $t_l^{\it start}$  ,  $t_l^{\it process}$  ,  $t_l^{\it deadline}$  denote the start time, processing time and deadline for task  $\it l$ 

L denotes the total number of tasks



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### Multi-Objective MILP Problem Constraints



Network Flow Constraints: Time-varying travel and usage cost

$$\sum_{t=1}^{T} \sum_{i \in Q(1,t)} x_{likt} = 1, \forall k$$

$$\sum_{t=1}^{T} \sum_{i \in P(N,t)} x_{iNkt} = 1, \forall k$$

$$\sum_{t=1}^{T} \sum_{i \in P(N,t)} x_{iNkt} = 1, \forall k$$

$$\sum_{t=1}^{T} \sum_{i \in Q(i,t)} x_{ijkt} - \sum_{t=1}^{T} \sum_{j \in P(i,t)} x_{jikt} = 0, \ \forall k, \forall i \neq 1 \& i \neq N$$

$$\sum_{t=1}^{T} \sum_{j \in Q(i,t)} x_{ijkt} - \sum_{t=1}^{T} \sum_{j \in P(i,t)} x_{jikt} = 0, \ \forall k, \forall i \neq 1 \& i \neq N$$

$$\sum_{t=1}^{T} \sum_{j \in Q(i,t)} x_{ijkt} \leq \sum_{t=1}^{T} \sum_{j \in P(i,t)} x_{jikt}, \forall k, \forall i \neq 1, \forall \tilde{T} < T$$

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1(*d*)

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#### Task Execution Constraints: Delay in meeting the task deadline

$$\begin{aligned} t_{kloc(l)}^{depart} \geq & t_{l}^{start} + t_{l}^{process}, \ \forall l, \forall k \in \Psi_{l}^{asgn} \\ t_{l}^{start} = & \max_{k \in \Psi_{l}^{asgn}} t_{kloc(l)}^{arrive}, \forall l \\ & \sum_{j \in P(loc(l),t)} \sum_{k=1}^{K} x_{jloc(l)kt} \leq q_{l}, \ \forall l, \forall t \end{aligned}$$

2(a) $t_{kloc(l)}^{depart}$  : Departure time of UAV k

2(b)  $t_{kloc(l)}^{arrive}$ : Arrival time of UAV k

 $\Psi_{l}^{asgn}$ : Set of assigned UAVs for task l

P(i,t): Predecessor cells of i at time t

 $q_l$ : Maximum number of UAVs for task l2(c)

loc(l): Location of task l

### Multi-Objective MILP Problem Constraints



Collision Avoidance Constraints: Ensures safe path by avoiding collision with obstacles

 $t_{k'i}^{arrive} - t_{ki}^{depart} \geq \Delta t - M\alpha_{kk'i} \ \forall i, k, k' \neq k \qquad \qquad 3(a) \qquad M \quad : \text{Large number}$   $t_{ki}^{arrive} - t_{k'i}^{depart} \geq \Delta t - M(1 - \alpha_{kk'i}) \ \forall i, k, k' \neq k \qquad \qquad 3(b) \qquad \alpha_{kk'i} \quad : \text{Binary variable indicating}$  when UAV k arrives after k'  $\alpha_{kk'i} \in \{0,1\}, \forall i, k, k' \neq k \qquad \qquad \Delta t \quad : \text{Time gap}$ 

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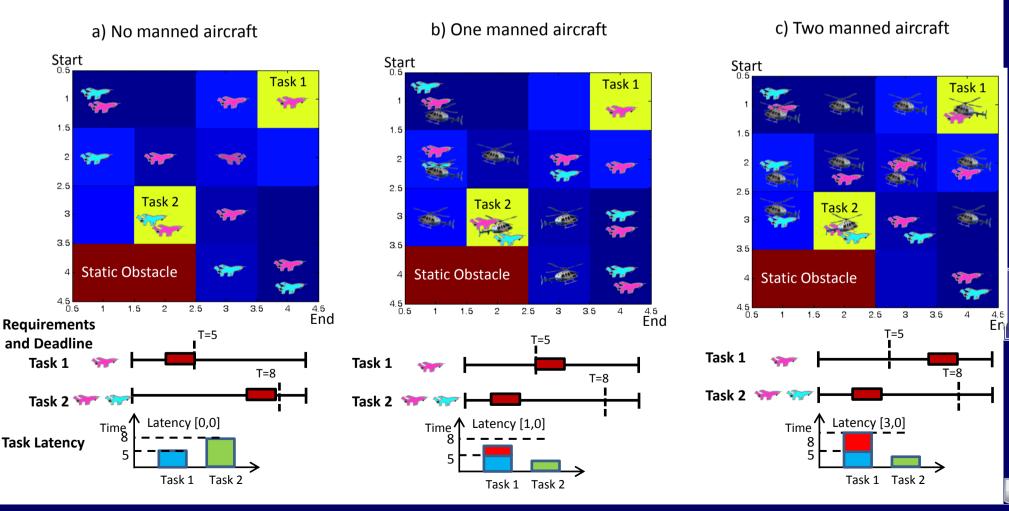


• Arrival and Departure Constraints: Tracks the execution status of tasks

$$t_{k1}^{arrive} = 0, \forall k \qquad \qquad 4(a)$$
 
$$t_{ki}^{depart} + t_{k}^{travel} x_{ijkt} \leq t_{kj}^{arrive} + M(1 - x_{ijkt}), \forall k, \forall i, \forall j \neq 1, \forall t \qquad 4(b) \quad \text{where}$$
 
$$t_{ki}^{depart} \geq t_{ki}^{arrive}, \ \forall i \notin \{loc(l)\}, \forall k \qquad \qquad 4(c) \quad t_{ki}^{depart} : \text{Departure time of UAV } k \text{ from cell } i$$
 
$$t_{ki}^{depart} \geq t_{ki}^{arrive}, \ \forall i \in \{loc(l)\}, \forall k \notin \Psi_{l}^{asgn} \qquad \qquad 4(d) \quad t_{ki}^{arrive} : \text{Arrival time of UAV } k \text{ at cell } i$$

### Multi-Objective UAV Path Planning Results

- **Solution**: Decomposed MILP solution approach:
  - Phase I: Minimize the path risk of each UAV given the estimated arrival time at each task location
  - Phase II: Minimize the task latency with respect to the arrival time of each UAV at each task location given the path in Phase I
- Scenario I: Coordinated path planning in different contexts



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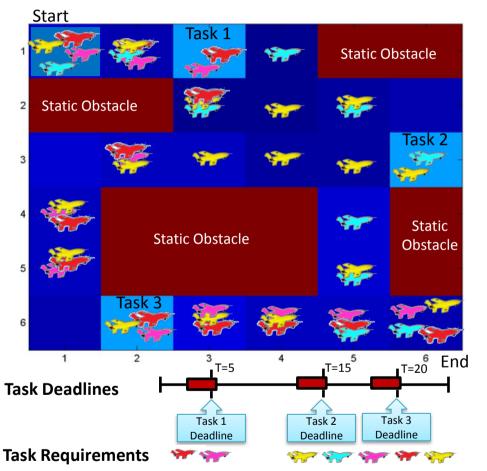
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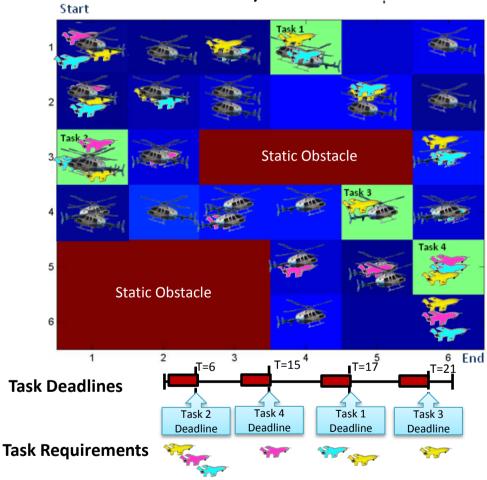
### Multi-Objective UAV Path Planning Results

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 Scenario II: Coordinated path planning around static obstacles



 Scenario III: Coordinated path planning around static and dynamic obstacles



- **Scenario I**: An increase in the number of manned aircraft delays the task processing time in order to guarantee safe trajectory planning within a confined mission area
- Scenario II & III: Mission tasks are completed on time in a large environment with static and dynamic obstacles

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### Python Implementation of 3D A\* Algorithm

• Given:

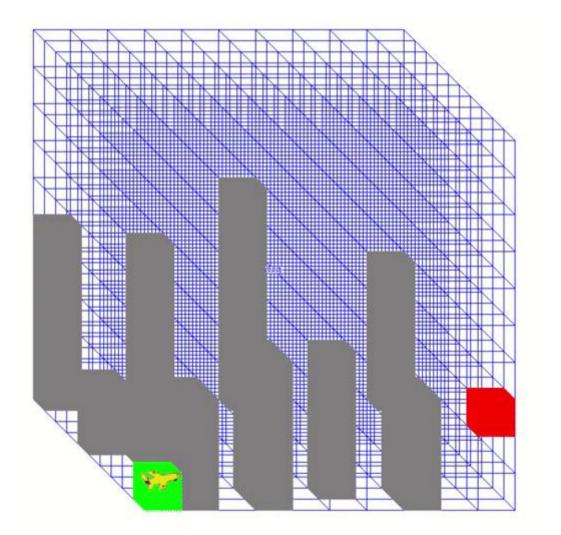
- Mission: Path planning

- Environment: 3D mission space

- Asset: UAV

- Task: Plan path from start point to end point while avoiding static obstacles

Future Work: 3D path planning for multiple UAVs within a dynamic environment









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## Python Implementation of 3D A\* Algorithm

• Given:

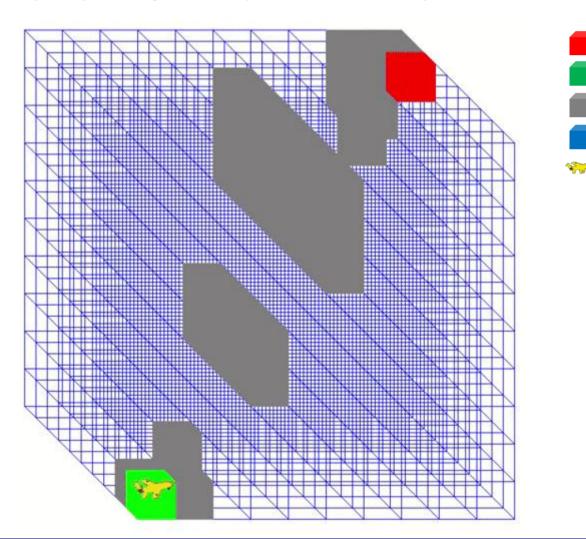
- Mission: Path planning

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Task: Plan path from start point to end point while avoiding static obstacles

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**End Point** 

**Start Point** 

**Obstacles** 

Path

UAV

Objectives & Constraints



### Conclusion

#### Summary

- UAVs are useful for dull, dirty, and dangerous military and civilian operations
- A multi-objective UAV path planning problem was investigated for coordinated task execution in a dynamic environment including:
  - Mathematical formulation of the path planning problem
  - A two-phase algorithm to solve the resulting MILP problem
- 3D A\* algorithm was implemented in Python

#### Future Work

- Explore approximation techniques, such as ant colony system and genetic algorithms
- Revise the current planning structure to a distributed setting
- Explore 3D path planning and address the vertical collision avoidance problem
- Incorporate pop-up threats and sudden UAV breakdown scenarios



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### Future UAV Mission Planning Challenges

#### **Future UAV Mission Planning Challenges**

- Provide capabilities more efficiently through modularity and interoperability
- Increase in autonomous *multi-platform control*
- More survivable with improved and resilient communications and security from tampering
- Efficient manned and unmanned teaming to reduce the number of personnel required to operate and maintain the systems
- Consider realistic models and incorporate/fuse data from different sources

#### **UAV Mission Planning Objectives**

- Dynamic coordination of multiple unmanned vehicles operating on ground, air, and water
- Develop efficient algorithms to mimic human-like behavior in unmanned aerial vehicles for proactive decision support
- Data protection and exploitation using High Performance Computing (HPC)
- Reduce operator workload by improving autonomy using hierarchical mission planning
- Improve data flow and standard message architectures for reliable communication

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#### **High Performance Computing Impacts**

- Provides a consolidated plug-and-play application architecture
- Improves scalability and feasibility for unmanned aerial system vendors
- Improved battle space awareness via tasking, collection, processing, exploitation, and dissemination (TCPED) processes, required to translate vast quantities of sensor data into a shared understanding of the environment
- HPC enables *cross domain data sharing* of information and adapts rapidly to changing threats
- HPC addresses the challenges in cloud computing and multilayer security, communications, open standards, data storage, cost, ease of technology insertion, etc.

Ref: Unmanned Systems Integrated Road map FY 2013-2038, Reference Number 14-S-0553

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